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## EXISTENCE, UNIQUENESS AND DECAY ESTIMATES ON MILD SOLUTIONS TO FRACTIONAL CHEMOTAXIS-FLUID SYSTEMS

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ABSTRACT. We investigate a fractional chemotaxis system coupled with the Navier–Stokes fluid in the whole space  $\mathbb{R}^N$  with  $N\geq 3$ . With the help an appropriate functional space, we develop a framework for a *unified* treatment of the existence, uniqueness and decay estimates of global mild solutions to this problem under the assumption that initial data are small enough.

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 $Key\ words\ and\ phrases.$  Fractional chemotaxis; fractional Navier–Stokes; global mild solution; decay estimates.

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