Topological Methods in Nonlinear Analysis Volume 55, No. 1, 2020, 85–103 DOI: 10.12775/TMNA.2019.061

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GLOBALLY ATTRACTIVE MILD SOLUTIONS FOR NON-LOCAL IN TIME SUBDIFFUSION EQUATIONS OF NEUTRAL TYPE

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ABSTRACT. We prove the existence of at least one globally attractive mild solution to the equation

 $\partial_t (b * [x - h(\cdot, x(\cdot))])(t) + A(x(t) - h(t, x(t))) = f(t, x(t)), \quad t \ge 0,$

under the assumption, among other hypothesis, that A is an almost sectorial operator on a Banach space X and the kernel b belongs to a large class, which covers many relevant cases from physics applications, in particular the important case of time-fractional evolution equations of neutral type.

1. Introduction

Existence of globally attractive solutions for mathematical models is a very challenging topic that is drawing the attention of many researchers in the last decade. For instance, Alzabut and Abdeljawad in [1] studied the existence of a globally attractive periodic solutions of an impulsive delay logarithmic population model. Bartuccelli, Deane and Gentile [3] analyzed globally and locally attractive solutions for quasi-periodically forced systems, and Li and Cheng [8] established conditions for the existence of globally attractive periodic solutions

 $^{2020\} Mathematics\ Subject\ Classification.\ 34K40,\ 34K37,\ 35R11,\ 45D05.$

Key words and phrases. Attractive mild solutions; non-local in time equations; neutral type equations; integral Volterra equations.

J. González-Camus was supported by ANID under grant Doctorado Nacional Chile 2016 Number 21160120.

C. Lizama is partially supported by FONDECYT grant number 1180041.