Topological Methods in Nonlinear Analysis Volume 54, No. 1, 2019, 153–175 DOI: 10.12775/TMNA.2019.032

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## SOLUTIONS FOR QUASILINEAR ELLIPTIC SYSTEMS WITH VANISHING POTENTIALS

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ABSTRACT. In this paper, we study the following strongly coupled quasi-linear elliptic system:

liptic system: 
$$\begin{cases} -\Delta_p u + \lambda a(x) |u|^{p-2} u = \frac{\alpha}{\alpha + \beta} |u|^{\alpha - 2} u |v|^{\beta}, & x \in \mathbb{R}^N, \\ -\Delta_p v + \lambda b(x) |v|^{p-2} v = \frac{\beta}{\alpha + \beta} |u|^{\alpha} |v|^{\beta - 2} v, & x \in \mathbb{R}^N, \\ u, v \in D^{1,p}(\mathbb{R}^N), & & x \in \mathbb{R}^N, \end{cases}$$

where  $N \geq 3$ ,  $\lambda > 0$  is a parameter,  $p < \alpha + \beta < p^* := Np/(N-p)$ . Under some suitable conditions which are given in section 1, we use variational methods to obtain both the existence and multiplicity of solutions for the system on an appropriated space when the parameter  $\lambda$  is sufficiently large. Moreover, we study the asymptotic behavior of these solutions when  $\lambda \to \infty$ .

<sup>2010</sup> Mathematics Subject Classification. Primary: 35H30, 35J20; Secondary: 35J45. Key words and phrases. Positive solutions; potential well; quasilinear elliptic systems. This work was partially supported by NSFC (No. 11301204, No. 11371159), self-determined research funds of CCNU from colleges' basic research and operation of MOE(CCNU16A05011).