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## TOPOLOGICAL ENTROPY OF DIAGONAL MAPS ON INVERSE LIMIT SPACES

Ana Anušić — Christopher Mouron

ABSTRACT. We give an upper bound for the topological entropy of maps on inverse limit spaces in terms of their set-valued components. In a special case of a diagonal map on the inverse limit space  $\lim_{I \to I} (I, f)$ , where every diagonal component is the same map  $g: I \to I$  which strongly commutes with f (i.e.  $f^{-1} \circ g = g \circ f^{-1}$ ), we show that the entropy equals  $\max{\text{Ent}(f), \text{Ent}(g)}$ . As a side product, we develop some techniques for computing topological entropy of set-valued maps.

## 1. Introduction

Topological entropy is one of the most popular (topological) measures of complexity of a dynamical system. It was introduced by Adler, Konheim and McAndrews [1] for compact topological spaces, and further refined by Bowen [4] and Dinaburg [8] in case of metrizable spaces. We are interested in describing entropy of maps on complicated spaces in terms of much simpler, one-dimensional maps.

The spaces we study can be described as *inverse limits* on compact, connected, metric spaces (often called *continua*)  $X_i$ ,  $i \ge 0$ , with continuous and

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