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## DECAY MILD SOLUTIONS OF FRACTIONAL DIFFERENTIAL HEMIVARIATIONAL INEQUALITIES

Xiuwen Li — Zhenhai Liu — Ricai Luo

ABSTRACT. The goal of this paper is to consider fractional differential hemivariational inequalities (FDHVIs, for short) in the framework of Banach spaces. Our first aim is to investigate the existence of mild solutions to FDHVIs by means of a fixed point technique avoiding the hypothesis of compactness on the semigroup. The second step of the paper is to study the existence of decay mild solutions to FDHVIs via giving asymptotic behavior of Mittag–Leffler function.

## 1. Introduction and problem formulation

As we known, differential variational inequalities (DVIs, for short) were firstly systematically discussed by Pang–Stewart [32] in Euclidean spaces. Some scholars have found that DVIs provide excellent tools to describe various models in mechanical impact problems in engineering, operations research, and physical sciences such as electrical circuits with ideal diodes, Coulomb friction problems

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