



Víctor Aranda 

RETRACTED ARTICLE: A Completeness Theorem for a Functionally Complete Łukasiewicz Logic

The Editors-in-Chief have retracted this article because, after publication, it became apparent that it cites Mateusz Radzki's paper (2017), which contains an error in the proof of the claim that Ślupecki's three-valued system is incomplete. Therefore, based on Radzki's paper, it cannot be concluded that Ślupecki's system is really incomplete. Although the results contained in Víctor Aranda's LLP paper are not formally dependent on the content of Radzki's text, we have decided to ask the author to withdraw the original submission and prepare its corrected version. The corrected version is available at <https://doi.org/10.12775/LLP.2026.010>

We want to express our profound gratitude to Professor Jan Zygmunt for his consultations and for pointing out the reference to Radzki's erroneous proof of claim that Ślupecki's system is incomplete.

Supplementary Information: The online version contains supplementary material available at <https://doi.org/10.12775/LLP.2025.014>

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